

Correction Super bonus.

Facteur $A = \underbrace{4(y-3)^2}_{=a^2} - \underbrace{25(1-y)^2}_{=b^2}$

$$\begin{aligned} A &= 2^2(2-y)^2 - 5^2(1-y)^2 \\ &= (2(2-y))^2 - (5(1-y))^2 \\ &= (2(2-y) + 5(1-y))(2(2-y) - 5(1-y)) \\ &= (4 - 2y + 5 - 5y)(4 - 2y - 5 + 5y) \\ &= \underline{(-7y + 9)(3y - 1)} \end{aligned}$$

$$\begin{aligned} B &= 3(4y+1)(3y-1) - \underbrace{(16y^2-1)}_{a^2-b^2} \\ &= 3(4y+1)(3y-1) - [(4y+1)(4y-1)] \\ &= 3(4y+1)(3y-1) - (4y+1)(4y-1) \\ &= (4y+1)[3(3y-1) - (4y-1)] \\ &= (4y+1)(9y-3-4y+1) \\ &= \underline{(4y+1)(5y-2)} \end{aligned}$$

Avec la propriété $\sqrt{a \times b} = \sqrt{a} \times \sqrt{b}$

$$\begin{aligned} C &= 12y^2 - 36y + 27 + (2y-3)(y+1) \\ &= (\sqrt{12}y)^2 - 36y + (\sqrt{27})^2 + (2y-3)(y+1) \end{aligned}$$

$$\sqrt{12} = \sqrt{3 \times 4} = \sqrt{3} \times \sqrt{4} = 2\sqrt{3}$$

$$\sqrt{27} = \sqrt{9 \times 3} = \sqrt{9} \times \sqrt{3} = 3\sqrt{3}$$

$$\text{donc } c = (2\sqrt{3}y)^2 - 36y + (3\sqrt{3})^2 + (2y-3)(y+1)$$

$$c = (2\sqrt{3}y - 3\sqrt{3})^2 + (2y-3)(y+1)$$

On vérifie que $2\sqrt{3}y \times 2 \times 3\sqrt{3} = 12\sqrt{3 \times 3}y = 12 \times 3 = 36y$

$$c = (\sqrt{3}(2y-3))^2 + (2y-3)(y+1)$$

$$= 3(2y-3)^2 + (2y-3)(y+1)$$

$$= 3(\underline{2y-3})(2y-3) + \underline{2y-3}(y+1)$$

$$= (2y-3)(3(2y-3) + (y+1))$$

$$= (2y-3)(6y-9 + y+1)$$

$$= \underline{(2y-3)(7y-8)}$$